

## TRANSPORT AND THERMOELECTRIC PROPERTIES OF $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ -Ag PERCOLATION SYSTEM

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Experimental studies on the transport and thermoelectric properties of  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ -Ag composite ceramic system have been performed and the results are analyzed from the viewpoint of the percolation theory. The percolation threshold volume fraction  $f_c$  of Ag determined from the electrical resistivity, thermal conductivity and Seebeck coefficient measurement is  $f_c=0.135\pm 0.005$ . This value is slightly smaller than the theoretical value  $f_c=0.16$  for three dimensional percolation in continuous media. The critical exponent  $t$ , which is defined by  $\sigma \propto (f_{\text{Ag}} - f_c)^t$  in the critical region above the percolation threshold  $f_c$ , is found to depend on the component conductivity ratio  $h = \sigma_{\text{YBCO}} / \sigma_{\text{Ag}}$ , which was varied by changing the oxygen deficiency  $\delta$ . This dependence of  $t$  on  $h$  can be understood on the basis of the scaling hypothesis. The behavior of the Seebeck coefficient is also analyzed on the basis of the percolation theory.

### 1. INTRODUCTION

One main hurdle against the application of high  $T_c$  oxide superconductors (HTSC) in ceramic forms is the occurrence of the weak-links at the border of grains, which practically limit the effective critical current  $I_c^{\text{eff}}$  of bulk cuprate superconductors. The addition of Ag metal to cuprates was found often to be effectual to make up for the weak-links and a good deal of the data on the transport properties of Ag doped HTSC have been accumulated just after the discovery of HTSC. It is surely physically interesting and also useful for applicational purpose to investigate the behavior of Ag clusters on the basis of the percolation theory. However, the accumulated data and analyses from the viewpoint of the percolation theory seem hitherto to be somewhat scattered and sometimes inconsistent each other.<sup>1-5</sup>

In this study, we try to develop synthetic analyses about the percolative behavior of Ag clusters in  $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$  (YBCO) by measuring the electrical resistivity, thermal conductivity and thermoelectric effect. The conductivity ratio of Ag metal and the cuprate is widely changed by varying the amount of oxygen deficiency  $\delta$  of YBCO. The

experimental results are analyzed on the basis of the scaling theory for the percolation of Ag clusters.

## 2. OUTLINE OF SCALING LAWS

In a two component random composite of  $M$  and  $I$ , clusters of  $M$  with infinite scale are at first formed when the volume fraction of  $M$  ( $f_M$ ) goes beyond a certain threshold value  $f_c$ . Assuming  $M$  to be a metal and  $I$  to be an insulator, a power law applies for the bulk effective conductivity  $\sigma_E$  of the composite;

$$\sigma_E = A\sigma_M(f_M - f_c)^t \quad \text{for } 0 < f_M - f_c \ll 1. \quad (1)$$

The values of  $t = 1.9 \pm 0.1$  and  $f_c \approx 0.16$  were predicted for the three-dimensional continuum media.<sup>6</sup> If  $I$  component is also somewhat conductive and the conductivity ratio  $h = \sigma_I / \sigma_M$  is not strictly zero, the power law of eq. (1) breaks down as  $\Delta f = f_M - f_c$  tends to zero. In this case,  $\sigma_E$  is expected to follow the scaling hypothesis,

$$\sigma_E = \sigma_M \Delta f^t \phi_+(z), \quad (2)$$

where  $z = h / \Delta f^{t+s}$ ,  $s (\approx 0.73)$  is the critical exponent governing the divergence of conductivity in a superconductor-metal composite for  $0 < f_M - f_c \ll 1$ . The universal scaling function  $\phi(z)$  can be explained in the power series of  $z$ :

$$\phi_+(z) = A + Bz + Cz^2 + \dots \quad \text{for } z < 1 \text{ and } f_M - f_c > 0. \quad (3)$$

For non-zero values of  $h$ , the conductivity data must be carefully handled taking proper account of region of  $z$  in which the application of eq. (3) is justified. In this paper,  $h$  dependence of the  $t$  exponent is mainly discussed.<sup>5,7</sup> The percolative behavior of the Seebeck coefficient is also investigated because it is an important parameter for practical application such as the thermoelectric refrigeration.<sup>8</sup>

## 3. EXPERIMENTAL

The Ag+ YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7- $\delta$</sub>  samples were prepared through the following procedure: YBCO powder and Ag<sub>2</sub>O powder (Dowa Mining Co. Ltd.) were mixed with an approximate weight ratio and pressed into pellets. The pellets were pre-sintered at 935°C for 15h in

air and furnace cooled. The pre-sintered pellets were crashed, mixed and again pressed into pellets. They were sintered at 930°C for 30h in air and then furnace cooled in 15h. After the obtained pellets were cut into square pillars ( $\sim 3 \times 3 \times 15 \text{ mm}^3$ ), they heated again and quenched into liquid  $\text{N}_2$  from various temperatures to prepare 'quenched samples'. The electrical resistivity was measured by a four-probe method between 10K to 260K using a GM refrigerator as a cryostat. The thermal conductivity  $\kappa$  and the Seebeck coefficient  $S$  were automatically measured in the same GM refrigerator.<sup>9</sup> The distribution of silver clusters was observed by a scanning electron microscope (SEM) and an electron probe microanalyzer (EPMA).

#### 4. EXPERIMENTAL RESULTS

Figure 1 shows the temperature dependence of the electrical resistivity  $\rho(T)$  of YBCO, non-quenched and quenched from 700°C, 800°C and 900°C.  $\rho(T)$  increases with increasing quenching temperature  $T_q$ . In the figure,  $\rho(T)$  of Ag+0.22at.%Au alloy whose residual resistivity ratio (RRR) is roughly equal to estimated RRR of Ag clusters in YBCO<sup>10</sup> is also shown. Figure 2 shows, as an example,  $\rho(T)$  of (Ag+YBCO) non-quenched samples for various Ag volume fractions  $f_{\text{Ag}}$  and Fig.3 shows the temperature

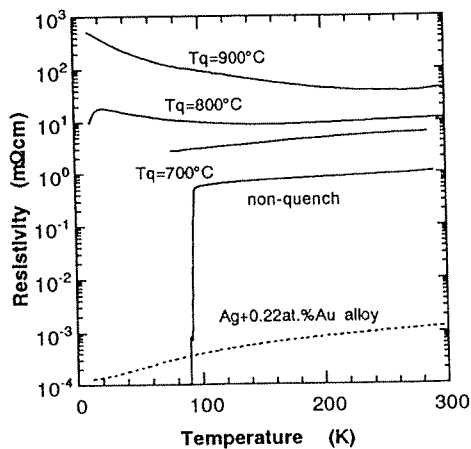


FIGURE 1

Temperature dependence of the electrical resistivity  $\rho(T)$  of YBCO non-quenched and quenched from 700°C, 800°C and 900°C.

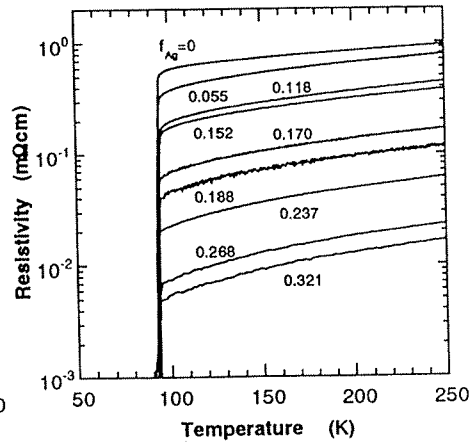


FIGURE 2

Temperature dependence of the electrical resistivity  $\rho(T)$  of (Ag+YBCO) non-quenched samples for various Ag volume fractions  $f_{\text{Ag}}$ .

dependence of the thermal conductivity  $\kappa(T)$  of  $(\text{Ag}+\text{YBCO})_{T_q=800^\circ\text{C}}$  for various  $f_{\text{Ag}}$ . As is expected,  $\rho(T)$  decreases and  $\kappa(T)$  increases with increasing  $f_{\text{Ag}}$ . Figures 4(a) and 4(b) show the temperature dependence of the Seebeck coefficient  $S$  of  $(\text{Ag}+\text{YBCO})_{T_q=900^\circ\text{C}}$  and  $(\text{Ag}+\text{YBCO})_{T_q=800^\circ\text{C}}$ , respectively.

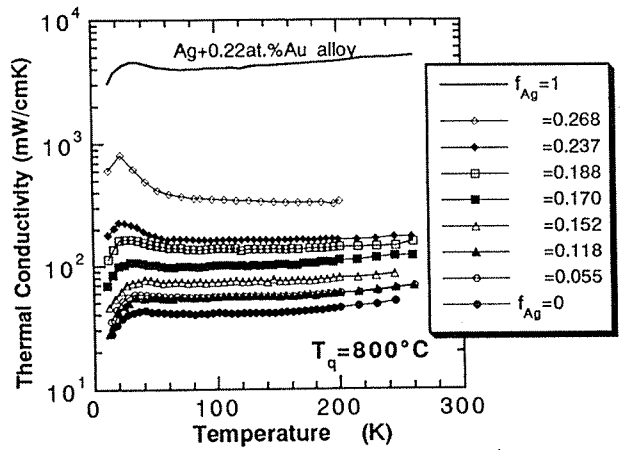


FIGURE 3 Temperature dependence of the thermal conductivity  $\kappa(T)$  of  $(\text{Ag}+\text{YBCO})_{T_q=800^\circ\text{C}}$  for various  $f_{\text{Ag}}$ .

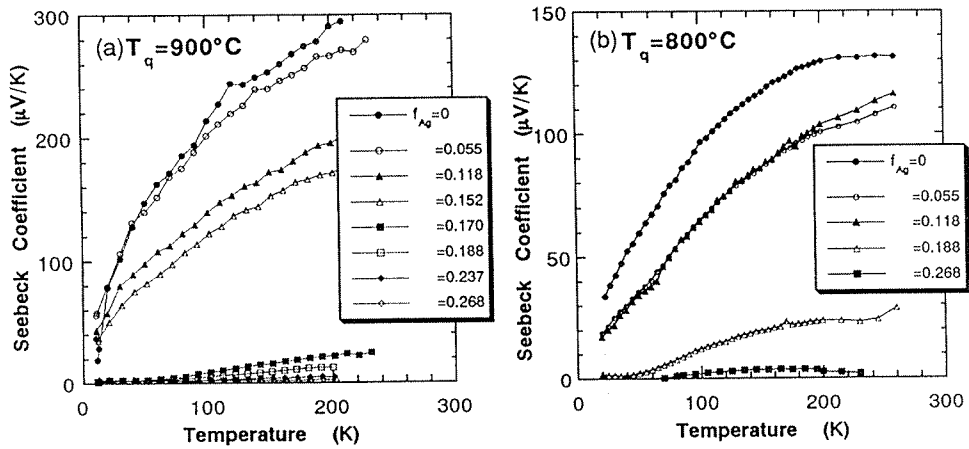


FIGURE 4 Temperature dependence of the Seebeck coefficient  $S$  of (a)  $(\text{Ag}+\text{YBCO})_{T_q=900^\circ\text{C}}$  and (b)  $(\text{Ag}+\text{YBCO})_{T_q=800^\circ\text{C}}$ .

## 5. DISCUSSION

Figures 5(a)-5(c) show the typical plots of  $\log \sigma_E$  vs  $\log (f_{Ag} - f_c)$  to determine experimental values of critical exponent  $t_{ex}$  and the percolation threshold  $f_c$ . The conductivity values at 150K were used because RRR of Ag cluster is verified to depend on  $f_{Ag}$  to some extent<sup>10</sup> and  $\sigma_{YBCO}/\sigma_{Ag}$  values become dependent on RRR of Ag cluster at low temperatures. The most suitable value of  $f_c$  was determined to be 0.135 for the present Ag+YBCO ceramics system. This  $f_c$  value is slightly smaller than the generally accepted value of  $f_c \approx 0.16$  for a 3D continuum media. The smaller value of observed  $f_c$  might reflect selective segregation of Ag clusters into grain boundary regions of YBCO. The determined  $t_{ex}$  values depend on the conductivity ratio  $h$  and are larger for smaller  $h$  as shown in Fig. 6. In the following, we estimate the relation between observed  $t_{ex}$  value and  $h$  on the basis of the scaling law given by eqs. (2) and (3).<sup>5,7</sup>

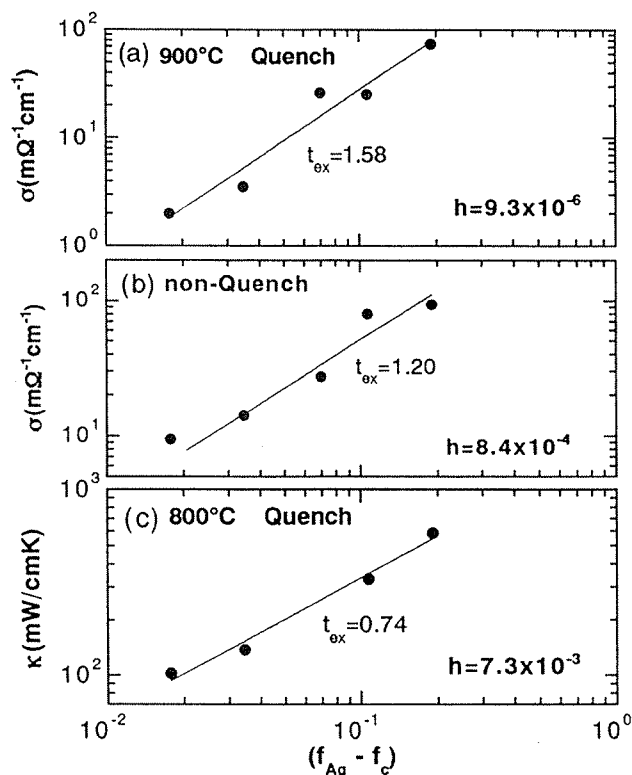


FIGURE 5 The typical plots of  $\log \sigma_E$  vs  $\log (f_{Ag} - f_c)$  to determine experimental values of critical exponent  $t_{ex}$  and the percolation threshold  $f_c$  for (a)  $T_q = 900^\circ\text{C}$ , (b) non-quenched and (c)  $T_q = 800^\circ\text{C}$ , respectively. Note that (c) is for the thermal conductivity.

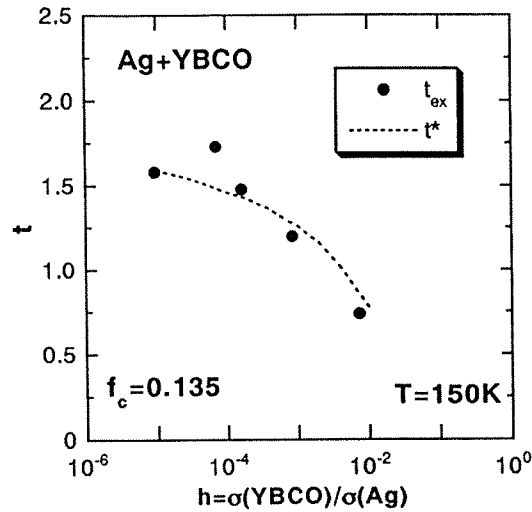


FIGURE 6 The experimentally determined  $t_{\text{ex}}$  values and calculated  $t^*$  values as a function of conductivity ratio  $h = \sigma(\text{YBCO})/\sigma(\text{Ag})$  (see text).

To calculate  $\sigma_E$  based on eq. (2), the scaling function  $\phi_+$  must be known. As a trial function, we set  $\phi_+(z) = A^+(1+z)$  and calculated  $\sigma_E$  in the range up to  $z=1$ . Then average slope between  $f_{\text{Ag}} - f_c = 0.2$  and  $z=1$  was defined as  $t^*$  and thus obtained  $t^*$  is given by the dotted line in Fig. 6. In the present calculation,  $t$  value of 1.8 and  $s$  value of 0.73 were used. We see in Fig. 6 that  $t^*$  values agree fairly well with experimental  $t_{\text{ex}}$  values. The parameter values used for the calculation are summarized in Table I.

Finally in Fig. 7 we plot  $\log(1/S)$  vs  $\log(f_{\text{Ag}} - f_c)$  for  $(\text{Ag} + \text{YBCO})_{T_{\text{q}}=900^\circ\text{C}}$  and  $(\text{Ag} + \text{YBCO})_{T_{\text{q}}=800^\circ\text{C}}$ .  $f_c$  value is set to be 0.135, the same value as the percolation threshold for the conductivity. The apparent value of the exponent  $t_{\text{ex}}$  is 1.59 and 1.90, respectively. These values almost coincide with  $t_{\text{ex}}$  values determined from the effective conductivity  $\sigma_E$ . The Seebeck coefficient can be expressed as

$$S = \frac{\pi^2}{3} \frac{k^2 T}{e} \frac{1}{\sigma} \frac{\partial \sigma}{\partial \varepsilon}, \quad (4)$$

where  $e$  is the electron charge and  $\varepsilon$  is the energy of electrons. Eq. (4) is inversely proportional to the conductivity  $\sigma$  and the experimental result that  $t_{\text{ex}}$  in the  $f_{\text{Ag}}$

dependence of  $S$  almost agrees to  $t$  determined from  $\sigma_E$  imply that the  $\partial\sigma/\partial\varepsilon$  term is nearly independent of the value of  $f_{Ag}$ .

Table I. The parameter values used for the calculation of  $t^*$  and experimental  $t_{ex}$  values.

measurement	$T_q$	conductivity at 150K	$h(=\sigma_{YBCO}/\sigma_{Ag})$	$t_{ex}$	$t^*$
$\kappa$	800°C	$\kappa_{Ag}=4300\text{mW/cmK}$ $\kappa_{YBCO}=31.3\text{mW/cmK}$	$7.3\times 10^{-3}$	0.74	0.78
$\rho$	non-Q	$\sigma_{Ag}=1621\text{m}\Omega^{-1}\text{cm}^{-1}$ $\sigma_{YBCO}=1.36\text{m}\Omega^{-1}\text{cm}^{-1}$	$8.4\times 10^{-4}$	1.20	1.27
$\rho$	700°C	$\sigma_{Ag}=1621\text{m}\Omega^{-1}\text{cm}^{-1}$ $\sigma_{YBCO}=0.26\text{m}\Omega^{-1}\text{cm}^{-1}$	$1.6\times 10^{-4}$	1.48	1.43
$\rho$	800°C	$\sigma_{Ag}=1621\text{m}\Omega^{-1}\text{cm}^{-1}$ $\sigma_{YBCO}=0.114\text{m}\Omega^{-1}\text{cm}^{-1}$	$7.0\times 10^{-5}$	1.73	1.49
$\rho$	900°C	$\sigma_{Ag}=1621\text{m}\Omega^{-1}\text{cm}^{-1}$ $\sigma_{YBCO}=0.015\text{m}\Omega^{-1}\text{cm}^{-1}$	$9.3\times 10^{-6}$	1.58	1.99

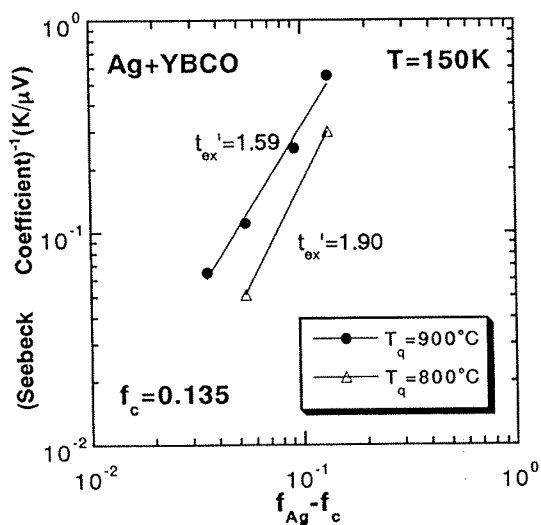


FIGURE 7 The plots of  $\log(1/S)$  vs  $\log(f_{Ag}-f_c)$  for  $(\text{Ag}+\text{YBCO})_{T_q=900^\circ\text{C}}$  and  $(\text{Ag}+\text{YBCO})_{T_q=800^\circ\text{C}}$  samples.

## 5. SUMMARY

(1) The electrical resistivity  $\rho$ , the thermal conductivity  $\kappa$  and the Seebeck coefficient  $S$  were measured for  $\text{Ag}+\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$  ceramics composite and the results were analyzed from the viewpoint of the percolation theory. The percolation threshold volume fraction  $f_c$  of Ag is determined to be 0.135, which is a little smaller than 0.16 generally accepted for random binary alloys in 3D continuum media.

(2) Observed critical exponent  $t_{\text{ex}}$  for  $f_{\text{Ag}} > f_c$  is dependent on the conductivity ratio  $h = \sigma(\text{YBa}_2\text{Cu}_3\text{O}_{7-x})/\sigma(\text{Ag})$ , which was varied by quenching the ceramics composite from various temperatures.

(3) The trial scaling function,  $\phi_+(z) = A(1+z)$  explains fairly well the  $h$  dependence of observed  $t_{\text{ex}}$  values.

(4) The critical exponent  $t_{\text{ex}}'$  of the Seebeck coefficient for  $f_{\text{Ag}} > f_c$  almost agrees to  $t_{\text{ex}}$  values determined from the electrical conductivity. This means that  $\partial\sigma/\partial\varepsilon$ , the electron energy dependence of the conductivity, is almost constant irrespective of the  $f_{\text{Ag}}$  values.

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